

A pure variation of risk in private-value auctions*

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Abstract

We introduce a new method of varying risk that bidders face in first-price and second-price private value auctions. We find that decreasing bidders' risk in first-price auction reduces the degree of overbidding relative to the risk-neutral Bayesian Nash equilibrium prediction. This finding is consistent with the risk-aversion explanation of overbidding. Furthermore, we apply the method to second-price auctions and find that bidding behavior is robust to manipulating bidders' risk as generally expected in auction theory.

Keywords: risk, first-price auctions, second-price auctions, risk-aversion, overbidding

JEL classification: C92, D44

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1 Introduction

Auction theory is a powerful economic tool. It is used to advise governments and businesses on designing and bidding in auctions (e.g., Cramton, 1995, or Milgrom, 2004). In many cases, however, auction designers and strategic advisors have complemented their auction theoretic analysis with an experimental examination to check for the behavioral robustness of the theoretic advice (e.g., Abbink et al., 2005, or McMillan, 1994). This additional information seems necessary because empirical and experimental research has uncovered systematic discrepancies between observed and expected behavior in auctions. While numerous additions to classical auction theory, especially alternative preference structures and stochastic choice models, have been proposed in the literature, so far, no attempt has been made to quantify the influence of any of the suggested effects. It is well known that classical auction theory is not fully in line with bidding behavior and it is also well known that a number of phenomena may play a role. It is not known, however, to which degree any of the suggested phenomena actually influence behavior.

In this paper we present a new experimental method that allows us to systematically quantifying the influence of risk preferences on bidding behavior. Bidders' non-neutral risk-preferences, especially their risk-aversion,¹ constitute one of the most prominent explanations of the gap between observed and predicted bidding behavior (Kagel, 1995). While a number of studies have demonstrated that risk-aversion alone is not sufficient to explain all deviations from risk-neutral Bayesian Nash equilibrium prediction in first-price private value auctions,² no study has yet quantified the extent to which risk-preferences affect bidding behavior, because "one element of the theory that cannot be replicated in an experiment is the risk neutrality of bidders, for the risk attitudes of the subjects cannot be controlled." (Andreoni et al. 2007, p. 246.)

The experimental protocol that we introduce allows us to control the amount of risk faced by bidders in first- and second-price sealed-bid auctions with private values. Hence, instead of measuring or inferring individual risk-preferences, we vary the risk in the auction situation systematically for all bidders, no matter which risk-preferences they have. This opens up the possibility to study to what extent risk-preferences explain bidding behavior and to what degree

¹The most widely propagated models of risk-averse bidders are the Constant Relative Risk-Aversion CRRA Model (Cox et al., 1988) and the Constant Absolute Risk Aversion (CARA) Model (Maskin and Riley, 1984; Matthews, 1987).

²Kagel and Levin (1993) find overbidding relative to the risk-neutral prediction in third-price auction experiments where risk-averse bidders are predicted to bid less than risk-neutral bidders. Chen and Plott (1998) show that the CRRA model is outperformed by a simple model with linear markdown bidders if values are not uniformly distributed as in most experiments. Kirchkamp and Reiss (2010) demonstrate that - if not precluded by the experimental design - a substantial amount of underbidding for low valuations can be observed, contradicting the notion of purely risk-averse bidders.

other factors are relevant. Once risk is eliminated from the auction situation, any discrepancy that remains between observed and predicted bidding cannot be attributed to risk-preferences. If observed and predicted behavior are indistinguishable after eliminating the risk, then risk-preferences seem to be sufficient to explain behavior. If discrepancies remain, we can establish the relative importance of risk attitudes compared to the influence of other factors.³

Specifically, we isolate the effect of risk experienced by bidders in first-price and second-price auctions in the presence of strategic uncertainty. We modify risk in a natural way by varying the number of income-relevant auctions that a participant plays with a given bidding strategy in each round. Our procedure is very different from the lottery payoff procedure that was first introduced by Roth and Malouf (1979) and first used in auction experiments by Cox, Smith, and Walker (1985). The lottery payoff procedure attempts to induce risk-neutral behavior by paying subjects in lottery tickets for a final "grand lottery." Since only the chances to win, but not the risk attached to the grand lottery is affected by the behavior in the experiment, expected utility maximizers have risk-neutral preferences with respect to the lottery payment. Selten, Sadrieh, and Abbink (1999), however, show that subjects' choices using this method exhibit even greater deviations from the risk-neutral behavior (and from expected utility maximization) than with a standard payment procedure.⁴ The reason for the failure of the lottery payoff procedure seems to be that subjects - in violation of the combined lottery reduction axiom - perceive the setup as highly risky, because the payoff uncertainty is not dissolved gradually, but at once and only after the final decision in the experiment. Our procedure avoids this problem, because there are no combined lotteries and each choice is immediately followed by feedback after each round.

We find that the reduction of non-strategic risk moves observed bids significantly closer to the risk-neutral Bayesian Nash equilibrium prediction in first-price auctions. Overbidding for high valuations is significantly reduced, just as underbidding for low valuations. Overall, risk-preferences explain overbidding by approximately 50%.

As a robustness test of our method to manipulate auction risk, we also consider second-price private-value auctions. In second-price auctions, bidders have a weakly dominant bidding strategy that is independent of risk considerations. We hypothesize that bidding behavior in these auctions is not affected by varying the level of risk. Indeed, we observe that reducing risk

³Numerous other factors have been proposed in the literature that may affect bidding behavior. For example, Armantier and Treich (2009) find that bidders underestimate winning probabilities and show that the provision of accurate winning probabilities partly explains overbidding. Morgan, Steiglitz, and Reis (2003) model spiteful bidding behavior. Selten and Buchta (1999), Ockenfels and Selten (2005) and Neugebauer and Selten (2006) investigate the effect of information feedback and directional learning. Crawford and Iriberri (2007) study the implications of level- k -thinking for auction settings. Engelbrecht-Wiggans and Katok (2007, 2008) and Filiz-Ozbay and Ozbay (2007) theoretically and experimentally study the role of regret.

⁴This, in fact, is well in line with the results of Cox, Smith, and Walker (1985).

does not affect bidding behavior in our second-price auction experiments. This result validates our method and, thus, confirms our findings on the differentiated effect of risk-preferences on bidding behavior in first-price auctions.

The plan of the paper is as follows: in section 2 we introduce the theoretical foundation for eliminating risk in private-value first-price auctions. Section 3 describes our experimental design and section 4 provides our main experimental findings. Section 5 concludes.

2 Theoretical considerations: Elimination of risk in first-price auctions

Consider a first-price auction with private values that are identically and independently distributed. In the Bayesian Nash equilibrium with a symmetric equilibrium bid function, bidders face risky income prospects due to uncertainty about competitors' private values. In this subsection we show that uncertainty of this type can be eliminated from the auction game independently of arbitrary individual risk preferences. We transform the uncertain auction game into a related auction game of certainty so that risk preferences become meaningless and players behave as if they were risk neutral in the original game. Intuitively, we achieve complete risk elimination by averaging auction play over an infinite number of independent auction games where any player's strategy is fixed across all of these games while players' private values are randomly determined over and over again. In the limit players' equilibrium payoffs are deterministic and equal to expected equilibrium payoffs of the game played only once with risk neutral preferences. Theorem 1 formalizes the intuition.

Theorem 1. *Let $\beta(v)$ denote the symmetric equilibrium bid function in Bayesian Nash equilibrium under risk neutrality in the standard one-shot first-price auction game Γ . Let $\Sigma(m)$ denote a new auction game with individual von Neumann-Morgenstern risk preferences where each player bids with a fixed bidding strategy in $m > 1$ independent shots of the standard auction game Γ such that any player's payoff in auction game $\Sigma(m)$ is given by the average gain obtained in all m one-shot auctions. For $m \rightarrow \infty$, the strategy profile in symmetric Bayesian Nash equilibrium with risk neutrality in the standard auction game Γ is a symmetric Bayesian Nash equilibrium strategy profile in game $\Sigma(m \rightarrow \infty)$ with arbitrary individual risk preferences.*

Proof. Consider a standard private-value first-price auction with n bidders each having arbitrary von Neumann-Morgenstern risk preferences. The utility function of a representative player 1 is denoted by $u_1(\cdot)$ such that $u_1' > 0$ and $u_1(0) = 0$. Assume that players' random values, $\vec{V} = (V_1, \dots, V_n)$, are independently and identically distributed according to a probability density function $f(v)$ with domain \mathcal{D} . Let $X_1(\vec{V})$ denote player 1's random gain from the auction given

that all players adhere to bidding strategy profile $\vec{b} = (b_1(V_1), \dots, b_n(V_n))$. By independently distributed values, player 1's expected auction gain can be written as

$$E[X_1(\vec{V})] = \int_{\mathcal{D}} f(v_1) E[X_1(\vec{V})|V_1 = v_1] dv_1.$$

According to the rules of the first-price auction, the high-bidder wins the auction and pays her bid implying $E[X_1(\vec{V})|V_1 = v_1] = \Pr\{\text{bid } b_1(v_1) \text{ wins}\} [v_1 - b_1(v_1)]$, therefore,

$$E[X_1(\vec{V})] = \int_{\mathcal{D}} f(v_1) \Pr\{\text{bid } b_1(v_1) \text{ wins}\} [v_1 - b_1(v_1)] dv_1.$$

Now suppose that all players bid according to strategy profile \vec{b} not only in a single auction but in m different standard one-shot auctions where for each player m values are independently drawn, a new one for each of m one-shot auctions. Further, assume that any player's payoff is equal to the average gain obtained in all m one-shot auctions. The average gain of player 1 is denoted by $W_1(\cdot)$ and given by

$$W_1(\vec{V}_1, \dots, \vec{V}_m) = \frac{\sum_{j=1}^m X_{1,j}(\vec{V}_j)}{m}.$$

The average gain $W_1(\cdot)$ is computed from a series of m independently and identically distributed random variables. Therefore, the law of large numbers is applicable and implies that average gain $W_1(\cdot)$ is deterministic in the limit, equalling expected value $E[X_1(\cdot)]$:

$$\lim_{m \rightarrow \infty} W_1(\vec{V}_1, \dots, \vec{V}_m) = \int_{\mathcal{D}} f(v_1) \Pr\{\text{bid } b_1(v_1) \text{ wins}\} [v_1 - b_1(v_1)] dv_1. \quad (1)$$

The maximization problem of player 1 when participating in m one-shot auctions with bidding strategy $b_1(\cdot)$ and receiving the average gain as payoff is given by

$$\max_{b_1(v_1)} \text{EU}[W_1(\vec{V}_1, \dots, \vec{V}_m)].$$

As the number of auctions approaches infinity, result (1) implies that the maximization problem simplifies to

$$\max_{b_1(v_1)} \text{EU}[E[X_1(\cdot)]] = u_1 \left(\int_{\mathcal{D}} f(v_1) \Pr\{\text{bid } b_1(v_1) \text{ wins}\} [v_1 - b_1(v_1)] dv_1 \right). \quad (2)$$

Since the utility function is upward-sloping, maximization problem 2 is solved by the same bidding strategy that also solves, for any value $v_1 \in \mathcal{D}$, the following set of maximization problems, each conditional on v_1 :

$$\max_{b_1} \Pr\{\text{bid } b_1 \text{ wins}\} [v_1 - b_1].$$

Since the preceding problem is the standard maximization problem faced in a single private-value first-price auction with risk-neutral preferences, it is shown that the equilibrium strategy profile in standard auction game Γ with risk-neutrality is an equilibrium strategy profile in auction game $\Sigma(m \rightarrow \infty)$ with with arbitrary risk-preferences. \square

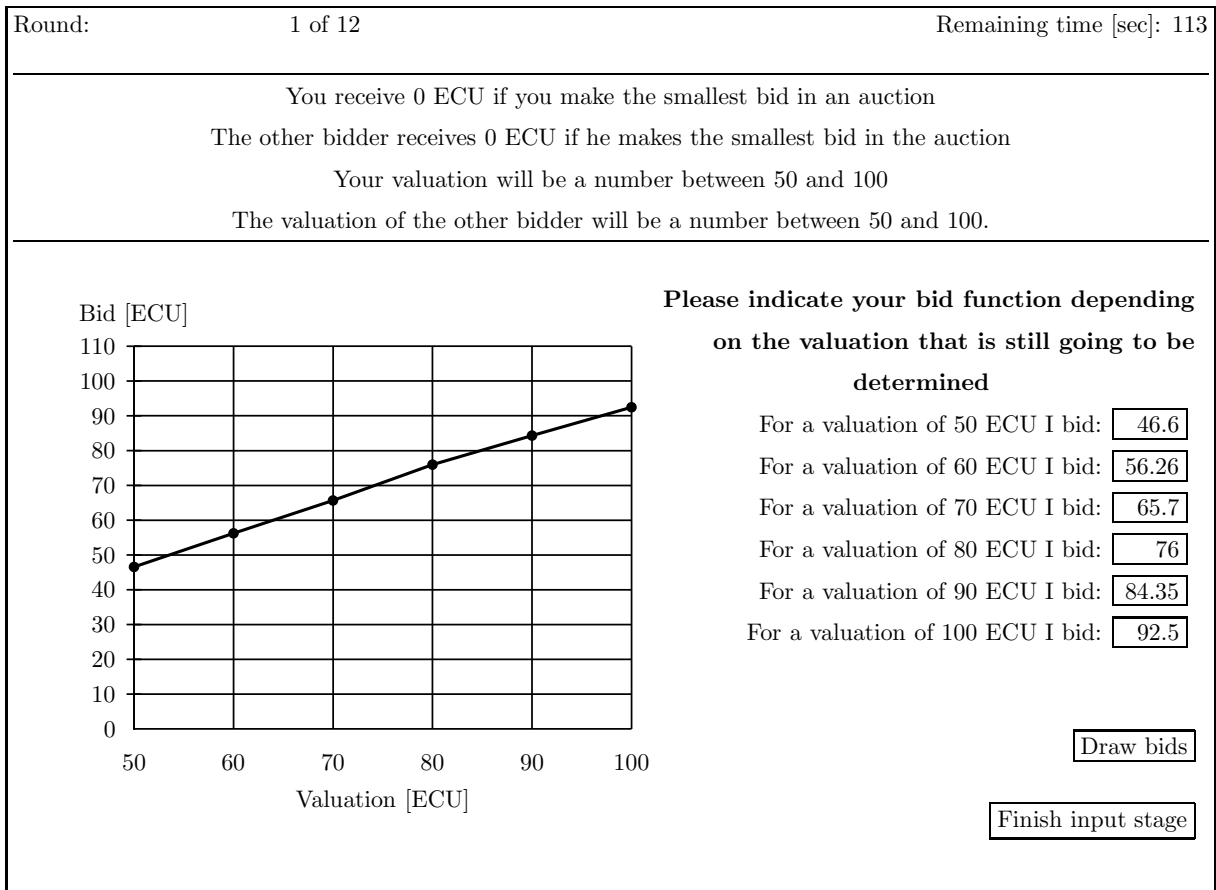


FIGURE 1: A typical input screen in the experiment (hypothetical data, translated into English)

Corollary 1. *If each player's utility function is characterized by constant relative risk aversion, i.e. $u_i(x) = x^{r_i}$, theorem 1 extends to the case where any player i 's payoff in game $\Sigma(m)$ is the sum of gains player i obtains in the m one-shot auctions.*

For risk-preferences consistent with, possibly heterogeneous, constant relative risk aversion (CRRA), corollary 1 extends the theorem to the case where any player's average payoff is replaced by the sum of gains in all individual one-shot auctions.

3 Experimental design and procedures

We implemented the auction of a single object with two bidders in the first-price or second-price sealed-bid design without reserve price. Experiments were conducted in June 2005 and May 2007 at the MaXLab at the University of Magdeburg. A total of 430 subjects participated in these experiments. All experiments were computerized with the software z-Tree (Fischbacher, 2007). We distributed written instructions to the participants and took questions in private. To ensure familiarity with the auction setting, subjects went through a short computerized quiz with standardized feedback before participating in the auction treatment.

TABLE 1: Treatment information

treatment	number of income-relevant auctions (A)	number of displayed auctions (G)	first-price (FP)	second-price (SP)	number of independent observations	number of subjects
A1G50FP	1	50	yes		6	54
A50G50FP	50	50	yes		6	56
A1G50SP	1	50		yes	9	72
A50G50SP	50	50		yes	9	72
control treatment						
A1G1FP	1	1	yes		6	48
A10G50FP	10	50	yes		6	56
A1G1SP	1	1		yes	9	72

Strategy method In the experiments we employed the strategy method to elicit bid functions. Selten and Buchta (1999) introduced the strategy method to experimental auctions. Subsequent studies, e.g., Pezanis-Christou and Sadrieh (2004) and Güth et al. (2002, 2003), applied it to various auction settings and obtained bidding data that assure the reliability of the more complex method of eliciting entire bid functions as opposed to eliciting a single bid for an assigned valuation. Our implementation of the strategy method follows Kirchkamp, Poen and Reiss (2009). In particular, we required participants to specify their bids for six different valuations (50, 60, ..., 100). Bids for valuations that were between those six valuations were obtained by linear interpolation. Figure 1 displays a typical input screen that participants faced to submit their bidding strategy in each round. This method to submit bidding strategies remained unchanged across all rounds and treatments.

Treatments In order to explore the role of risk preferences in private-value auctions, we consider three treatment variables: the number of income-relevant auctions (A), the number of auctions whose outcome is displayed to participants as feedback (G), and the auction format which is either first-price (FP) or second-price (SP). Table 1 summarizes parameter details of each treatment. Each treatment was divided into twelve rounds. In each round each participant was randomly matched with one other participant and used the submitted bidding strategy against her matched competitor in a fixed number of auction games. The number of played auction games per round was either one or fifty⁵ depending on the treatment. For every single auction game in any round, the valuation assigned to each participant was independently drawn from a uniform distribution with domain [50, 100]. A subset of all displayed auction games was selected at random to determine round income as the sum of all gains in the corresponding

⁵We strived for using the largest number of auctions that subjects could reasonably absorb on one feedback screen, see Figure 2.

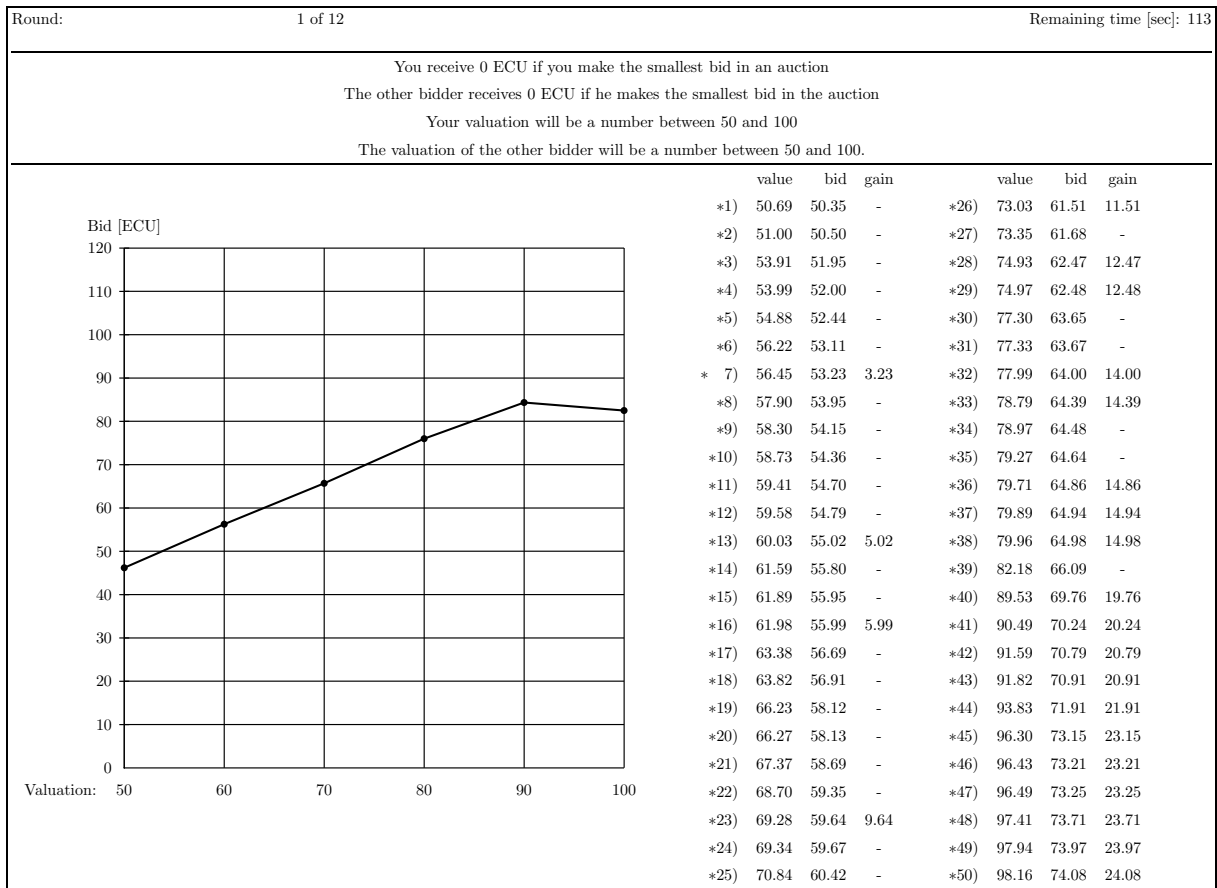


FIGURE 2: A typical feedback screen in the experiment (A50G50FP, hypothetical data)

individual auction games. The number of selected auctions that was relevant for income determination was either one or fifty. If an auction outcome was selected as income-relevant, it was marked with an asterisk in the feedback screen. To check how fast risk is eliminated we ran control-treatment A10G50FP with ten income-relevant auctions.

Multiple feedback on auction outcomes Figure 2 illustrates a typical feedback screen used in treatment A50G50FP where participants played 50 different auction games per round. The outcomes in all of these auctions were used to compute round income. Analogously, in the treatments with one income-relevant auction where 50 auctions were played, a single auction game was randomly selected and its outcome determined total round income. Figure 3 shows a typical feedback screen used in treatment A1G1FP with a single auction game played per round.⁶

⁶Subsequent to the first version of our working paper, Kirchkamp, Reiss and Sadrieh (2006), Engelbrecht-Wiggans and Katok (2009) reported the results of a related first-price auction experiment that differed in several ways. In particular, subjects bid against computerized bidders and were informed about the probabilities of winning the auction. For this aspect of the experimental design, Armantier and Treich (2009) find that the provision of winning probabilities affects bidding behavior such that bids are much closer to the risk-neutral

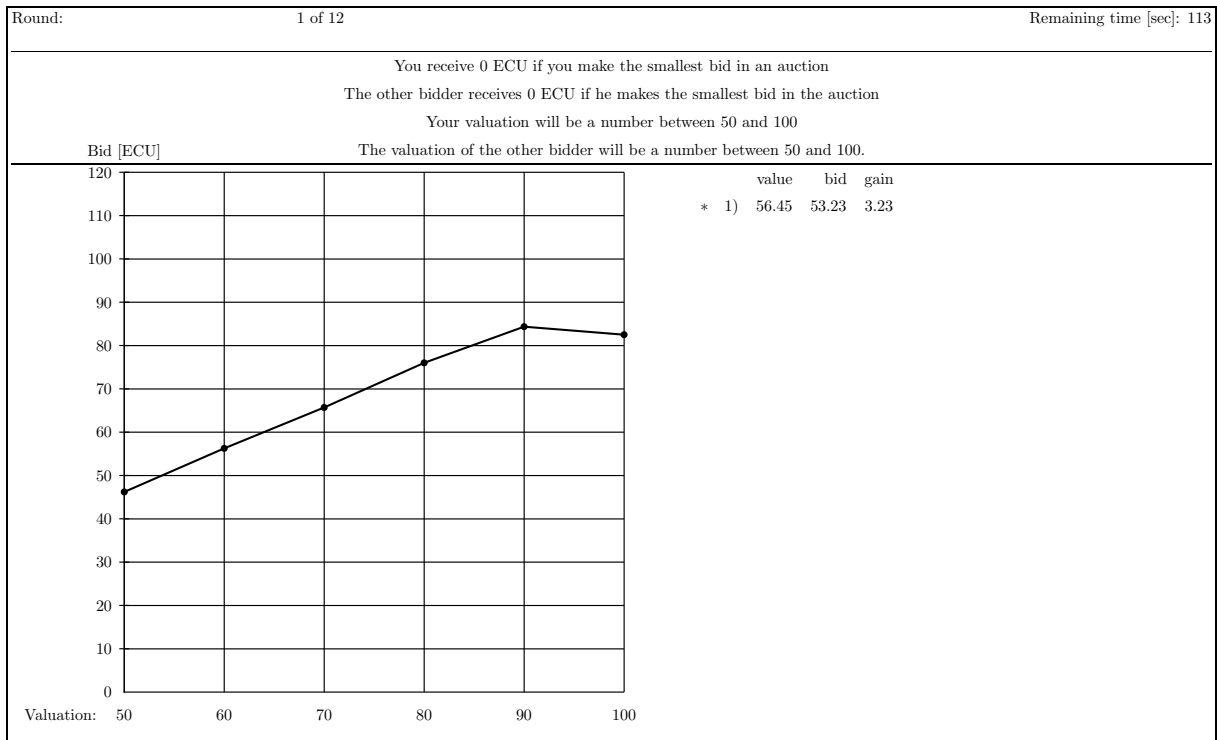


FIGURE 3: A typical feedback screen in the experiment (treatment A1G1FP, hypothetical data)

4 Experimental results

We first present the effects of manipulating risk on bidding behavior in first-price and second-price auctions in section 4.1. Next we report how bidding behavior responds to extensive variations of feedback in section 4.2. Then, we argue that the choice of 50 income-relevant auctions is a conservative one for our subjects to perceive the auction setting as essentially free of risk in section 4.4.

All results reported in section 4 use data from the entire experiment. Typically the first few rounds of auction experiments are characterized by particularly strong fluctuations of bidding activity. In response, we investigate bidding dynamics over time and find that our main results are robust to them, see appendix A.1. In appendix A.2 we complement the subset of our main results given on the aggregate level with an examination on the individual level suggesting robustness also to this end.

prediction. This behavioral effect together with the limited number of participants may explain why Engelbrecht and Wiggins (2009) do not find significant differences when varying the number auctions used for a rounds income computation.

4.1 The effects of reducing risk

Most importantly, we manipulated risk that bidders face in auctions. We essentially eliminated it by increasing the number of auctions that a bidder played with the same bidding strategy against the same opponent, but with different draws of the own and the opponent's valuations. The outcomes of a subset of all of these played auctions determined the round income of participants.

Irrespective of the auction rule, first-price or second-price, in treatments A1G50 and A50G50 every participant played 50 auctions in each round of the experiment with the same bidding strategy. In treatment A1G50 a single auction out of 50 played auctions was selected at random. The outcome of the selected auction entirely determined the participant's round income. In contrast, in treatment A50G50 all 50 auctions were selected to determine the participant's round income. Evidently, risk is much smaller if 50 different auction outcomes based on 50 different own and opponent's valuations determine round income instead of exclusively hinging on a single outcome.

4.1.1 First-price auctions

Under the first-price rule in Bayesian Nash equilibrium, any decrease in risk induces risk-averse bidders to bid closer to the risk-neutral equilibrium bid function. If risk disappears entirely, even a very risk-averse bidder bids as if having risk-neutral preferences by specifying the risk-neutral equilibrium bid function. Consequently, the theoretical predictions for risk-averse equilibrium in the reduced risk treatment (A50G50FP) are closer to risk-neutral equilibrium than in the standard risk treatment (A1G50FP). Therefore, if overbidding is due to risk aversion, we should expect more overbidding in the standard risk treatment (A1G50FP) than in the treatment with reduced risk (A50G50FP).

In our experiments we observe bid functions as opposed to single bids. This allows us to measure overbidding on the entire valuation domain. To quantify overbidding we use the area between the observed bid function and the risk-neutral equilibrium bid function. This concept naturally extends the standard approach of measuring overbidding as the difference of observed bid and risk-neutral equilibrium bid to the case of bid functions. Following the conventional approach, we ignore bids smaller than the risk-neutral prediction when studying overbidding. Therefore, our overbidding measure of bidder i in round t is given by:

$$A_{i,t}^+(b_{i,t}, \beta^{\text{RNBNE}}) = \int_{50}^{100} \max\{0, b_{i,t}(v) - \beta^{\text{RNBNE}}(v)\} dv,$$

For interpreting values of area measure A^+ , note that infinite risk-aversion, i.e. $b(v) = v$, leads to $A^+ = 625$ ECU; (it equals 50 ECU if observed bids exceed risk-neutral equilibrium bids by 1 ECU for any valuation v .)

The left panel of Figure 4 shows histograms of individual overbidding in the first-price treatments with reduced risk (dark bars) and standard risk (light bars) using overbidding measure $A_{i,t}^+$; the right panel depicts corresponding cumulative distribution functions. There is a large

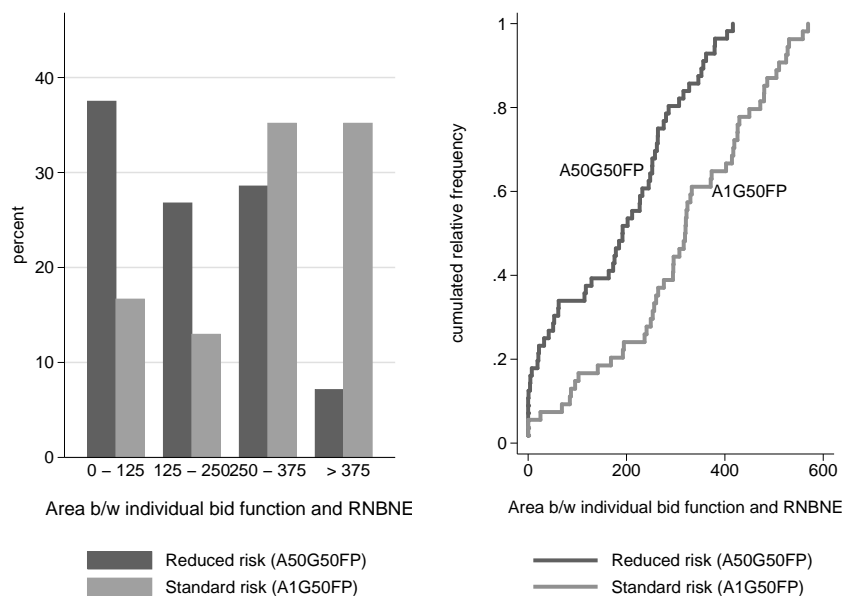


FIGURE 4: Overbidding response in first-price auctions when reducing risk

amount of overbidding in the standard risk treatment where the individual area measures of overbidding range from 0 to 569.17 ECU. With standard risk, 70.4% of bidders exhibit an overbidding measure larger than 250 ECU. In contrast, large overbidding of this magnitude applies to only 35.7% of bidders in the reduced risk treatment. Further, in the standard risk treatment, there are 35.2% of bidders with overbidding measures exceeding 375 ECU while there are only 7.1% of bidders showing similarly large overbidding in the reduced risk treatment. The lower frequency of large overbidding in the reduced risk treatment is reflected in the higher frequency of small amounts of overbidding; in the standard risk treatment only 29.3% of bidders exhibit an overbidding measure smaller than 250 ECU while there are 64.3% of bidders with a similarly small overbidding measure in the reduced risk treatment. Evidently, reducing risk shifts mass of the overbidding distribution to the left so that there is less overbidding with less auction risk. A Kolmogorov-Smirnov test confirms significant differences between both distributions ($p = 0.026$). We apply this and all other tests (including the t -test) on averages on independent observation level. Summary statistics for the area measure of overbidding are provided in Table 7 in the appendix.

To quantify the amount of overbidding that is attributable to the risk-aversion hypothesis, we regress the amount of overbidding A^+ on a constant and a treatment dummy D^{rr} following

equation (3) for treatments A1G50FP and A50G50FP. The dummy variable indicates if the observation was in the reduced risk treatment ($D^{\text{rr}} = 1$) or in the standard risk treatment ($D^{\text{rr}} = 0$). Calculations of standard errors are robust and take into account that observations might be correlated within matching groups but not across matching groups (Rogers, 1993). Results are summarized in Table 2.

$$A_{i,t}^+ = \beta_o + \beta_D D_{i,t}^{\text{rr}} + u_{i,t} \quad (3)$$

According to the regression results, our area measure of overbidding is 336.9 ECU with standard risk. As soon as risk is eliminated from the auction setting, overbidding falls by 135.6 ECU. Hence, the risk-aversion hypothesis explains 40.3% of overbidding in our standard risk treatment (A1G50FP); this is significantly different from zero (two-tailed t -test. $p = 0.002$).

explanatory variable	coefficient $\hat{\beta}$	robust σ_{β}	t	$P > t $
constant	336.930	25.424	13.25	0.000
D^{rr}	-135.566	33.280	-4.07	0.002

TABLE 2: Estimation of equation (3)

Finding 1. *Reducing risk in first-price private value auctions leads to less overbidding relative to risk-neutral Bayesian Nash equilibrium, supporting the risk-aversion hypothesis.*

Next we consider the impact of reducing risk on the average bid function to explore whether overbidding reductions are of local or global nature. For comparison of aggregate bidding behavior in the experiment and the risk-neutral equilibrium benchmark, consider the left panel of Figure 5. It depicts the average bid functions observed in the first-price treatments with standard risk (A1G50FP) and reduced risk (A50G50FP) together with the risk-neutral equilibrium bid function.⁷ As can be seen, the average bid function in the standard risk treatment (A1G50FP) is above the risk-neutral equilibrium bid function except for small valuations. This indicates that our collected first-price data for standard risk share the robust findings of underbidding for small valuations and overbidding for the residual set of valuations reported elsewhere; e.g., Cox et al. (1982), Kagel, Harstad and Levin (1987), Kagel (1995), Güth et al. (2003), and Kirchkamp and Reiss (2004).

Importantly, the average bids presented in the left panel of Figure 5 and detailed in Table 3 show that increasing the number of income-relevant auctions from 1 to 50 shifts the average bid function downward so that bidding is less aggressive with reduced risk. The effect of smaller bids with less risk is statistically significant.⁸

⁷Average bids are computed as the average of bids over the respective independent observations and the total

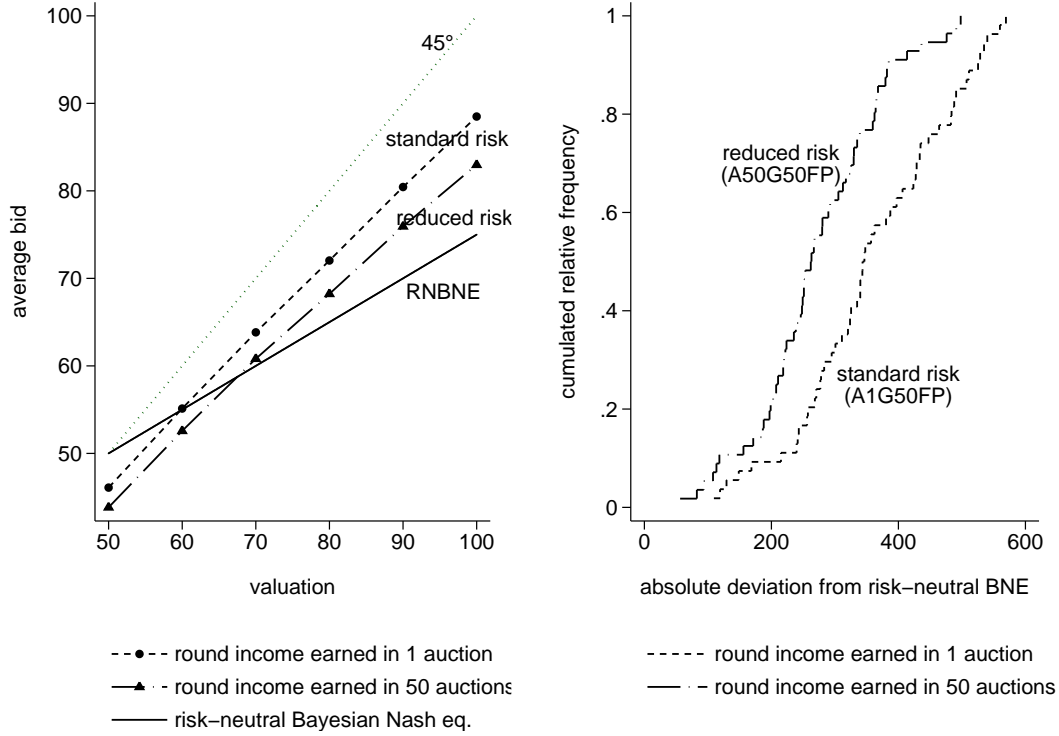


FIGURE 5: Bidding strategy effect in the experiment if the number of auctions played with the same bidding strategy increases under the first-price auction format.

Left panel: Average bid functions. Right panel: Cumulative frequencies of individual absolute deviations from risk-neutral equilibrium $A_{i,t}$.

The effect of reduced risk on absolute deviations from risk-neutral equilibrium as shown in Figure 5 is ambiguous. On the one hand, underbidding for small valuations appears to increase with reduced risk so that deviations ceteris paribus increase. On the other hand, the reduction of overbidding ceteris paribus reduces deviations. We quantify the individual net effect of reduced risk on risk-neutral equilibrium deviation as the area between any observed bid function for bidder i in period t and the risk-neutral equilibrium function:

$$A_{i,t}(b_{i,t}, \beta^{\text{RNBNE}}) = \int_{50}^{100} |b_{i,t}(v) - \beta^{\text{RNBNE}}(v)| dv.$$

The last column of Table 3 provides the average distance between bid functions observed in the first-price treatments and the risk-neutral equilibrium prediction using area measure $A_{i,t}$. With less risk (A50G50FP) observed bid functions are significantly closer to the risk-neutral prediction

number of periods.

⁸This is revealed by comparisons of average bids in the standard risk treatment (A1G50FP) to those in the reduced risk treatment (A50G50FP) using non-parametric Mann-Whitney- U -tests separately for each valuation (two-tailed, $p \leq 0.0374$); similarly, t -tests identify significant differences of average bids across treatments (two-tailed, $p \leq 0.0292$).

TABLE 3: Average bids in the first-price auction

valuation	50	60	70	80	90	100	$A(b, \beta^{\text{RNBNE}})$
β^{RNBNE}	50.0	55.0	60.0	65.0	70.0	75.0	0.0
A1G50FP	46.1	55.1	63.8	72.0	80.4	88.5	356.3
	(1.10)	(1.42)	(1.99)	(2.74)	(2.78)	(2.81)	(63.52)
A50G50FP	43.8	52.6	60.8	68.2	75.9	83.0	271.9
	(1.85)	(2.00)	(1.87)	(2.24)	(2.29)	(2.53)	(31.10)

Note: Standard deviations in parenthesis.

so that there are less deviations overall (two-tailed Mann-Whitney- U -test, $p = 0.0374$; two-tailed t -test, $p = 0.0153$).

Further, the right panel of Figure 5 depicts cumulative distributions of individual absolute deviation averaged over rounds for treatments A1G50FP and A50G50FP using area measure $A_{i,t}$. It can readily be seen that increasing the number of income-relevant auctions shifts the cumulated frequencies to the left implying substantially less deviations and less overbidding. A Kolmogorov-Smirnov test on the level of independent observations confirms that both distributions are significantly different from one another ($p = 0.026$). Reducing risk moves observed bid functions closer to risk-neutral equilibrium.

Finding 2. *Reducing risk in first-price private value auctions leads to smaller bids and less deviations from risk-neutral Bayesian Nash equilibrium.*

4.1.2 Second-price auctions

In the second-price auction, the symmetric equilibrium bidding strategy is not affected by manipulations of risk since it is weakly dominant, $\beta^{\text{WDS}}(v) = v$. Therefore, we hypothesize to observe no difference in bidding behavior between the standard risk treatment (A1G50SP) and the reduced risk treatment (A50G50SP). Figure 6 illustrates data for the second-price treatments with standard risk (A1G50SP) and reduced risk (A50G50SP). The left panel presents average bid functions. The right panel depicts cumulative distributions of individual deviations of observed bidding strategies from the weakly dominant equilibrium strategy using area measure $A_{i,t}$. In contrast to our first-price treatments, we do not find a treatment effect of average bids with reduced risk. For small valuations, average bids in the standard risk treatment (A1G50SP) are slightly larger than in the reduced risk treatment (A50G50SP), for larger valuations there is either no visible difference between average bids or the average bid in the standard risk treatment is larger. Table 4 summarizes data on average bids. Testing for treatment effects of average bids conditional on valuation does not reveal significant differences (two-tailed

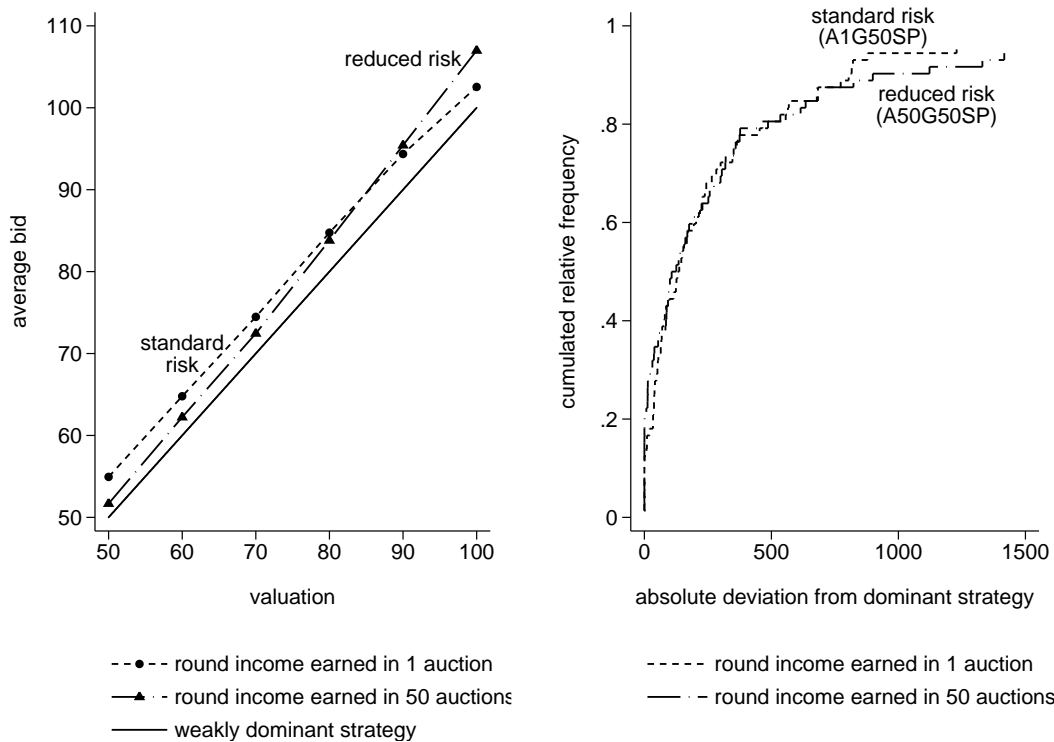


FIGURE 6: Bidding strategy effect in the experiment if the number of auctions played with the same bidding strategy increases under the second-price auction format.

Left panel: Average bid functions. Right panel: Cumulative frequencies of individual absolute deviations from weakly dominant strategy $A_{i,t}$.

Mann-Whitney- U -tests, $p \geq 0.2697$; two-tailed t -tests, $p \geq 0.2195$).

The average bid functions depicted in Figure 6 and the data given in Table 4 indicate that our data are characterized by widespread overbidding in the sense of bids exceeding valuations. This finding is widely documented for second-price auctions, though not conclusively understood, see, e.g., Andreoni, Che and Kim (2007), Cooper and Fang (2008), Güth et al. (2003), Kagel (1995), Kagel, Harstad and Levin (1987), Kagel and Levin (1993), and Garratt, Walker and Wooders (2004). Interestingly, our results are inconsistent with possible risk-based explanations of overbidding in second-price auctions since the level of risk appears not to be a major determinant of bidding behavior: The areas between individual bidding strategies and the weakly dominant strategy observed in both treatments (last column of Table 4) do not statistically differ from one another (two-tailed Mann-Whitney- U -test, $p = 0.8946$; two-tailed t -test, $p = 0.9297$). Further, the treatment distributions of individual absolute deviations between equilibrium and observed bidding strategies virtually coincide as the right panel of Figure 6 shows. Here, a Kolmogorov-Smirnov test on the independent observation level fails to identify significant differences ($p = 0.730$).

TABLE 4: Average bids in the second-price auction

valuation	50	60	70	80	90	100	$A(b, \beta^{\text{WDS}})$
β^{WDS}	50.0	60.0	70.0	80.0	90.0	100.0	0.0
A1G50SP	54.9	64.8	74.5	84.8	94.4	102.6	313.02
	(5.80)	(5.18)	(4.79)	(4.83)	(4.80)	(6.56)	(183.09)
A50G50SP	51.7	62.2	72.5	83.8	95.4	107.0	322.22
	(5.00)	(3.95)	(4.16)	(4.85)	(8.25)	(9.35)	(247.49)

Note: Standard deviations in parenthesis.

Finding 3. *Reducing risk in second-price private value auctions does not affect bidding behavior. The empirical regularity of overbidding valuations in second-price auctions is robust to manipulations of risk.*

4.2 The effects of information feedback about multiple auction outcomes

The standard first-price or second-price auction experiment informs individual bidders about the outcome of a single auction after bidding with an assigned private value and before bidding with a newly assigned private value in the next round of the experiment. Although learning opportunities are limited with repeated single bid-value experiences, bidding behavior is found to respond.⁹ Nevertheless, outcome feedback does not reduce deviations from the risk-neutral equilibrium prediction, neither in first-price nor second-price auctions.¹⁰

In comparison to single outcome feedback in any round, our feedback on 50 different auction outcomes for a given pair of bidders with fixed bidding strategies is extensive. It provides participants with ample opportunities to assess the consequences of multiple bid-value combinations where values are distributed over the entire valuation domain at the same time. Since the amount of feedback given in our treatments substantially differs from traditional feedback conditions we investigate if our findings regarding the effects of risk manipulation are robust to extensive feedback.

4.2.1 First-price auctions

A priori one might expect that if the introduction of extensive feedback has any influence on bidding behavior, then it leads participants to learn to avoid costly mistakes and to bid closer

⁹Experimental studies analyzing the effects of information feedback include Isaac and Walker (1985), Selten and Buchta (1999), Güth et al. (2003), Ockenfels and Selten (2005), Brosig and Reiss (2007), and Engelbrecht-Wiggans and Katok (2008).

¹⁰See, in particular, Güth et al. (2003) exploring learning effects in first-price and second-price auctions.

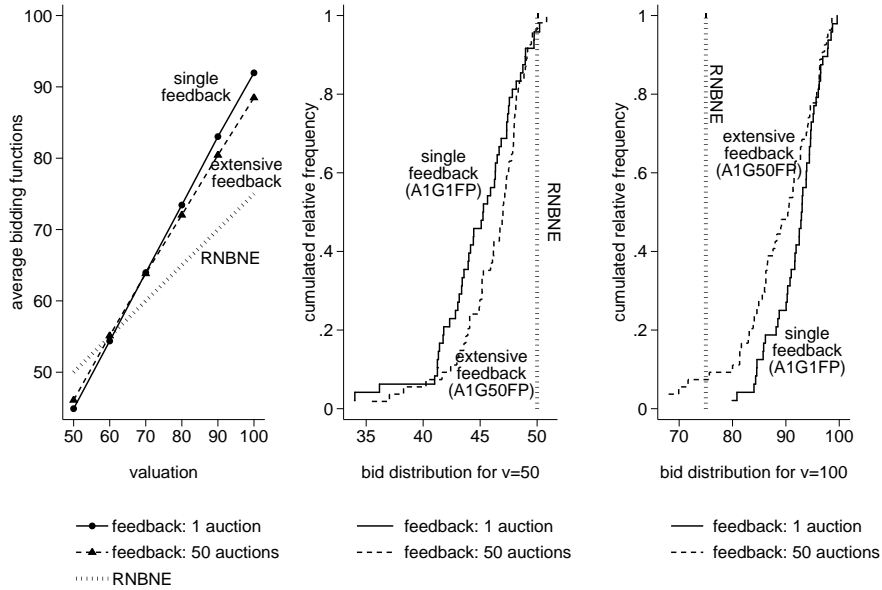


FIGURE 7: Feedback effect in the experiment if the number of auctions displayed is manipulated

to the risk-neutral equilibrium. For an impression whether multiple feedback has any effect on bidding behavior in first-price auctions, see the left panel of Figure 7 depicting average bid functions for treatments A1G1FP and A1G50FP; Table 5 details average bids. As can be seen in the Figure, average bids with single feedback (A1G1FP) are very close to average bids with extensive feedback. Nevertheless, the treatment difference of average bids is somewhat larger at the boundaries of the valuation domain. In particular the average bid with single feedback for the largest valuation of 100 is larger than that with extensive feedback implying less overbidding with extensive feedback. In contrast, the average bid with single feedback for the smallest valuation of 50 is slightly smaller than that with extensive feedback pointing to less underbidding for small valuations with extensive feedback.

The finding that feedback slightly reduces overbidding for large valuations and underbidding for small valuations does not only hold for average bids on the treatment level but also for the entire distribution of individually observed bid functions. To see this, Figure 7 graphs bid distributions for both feedback treatments where bids for each individual are averaged over all periods. For 98 out of 102 bidders the average bid observed for the smallest valuation of 50 ECU (middle panel) is smaller than the equilibrium bid of 50 ECU independently of the feedback condition. Importantly, the distribution of bids with extensive feedback strictly dominates the distribution with single feedback (in the sense of stochastic first-order dominance) so that there is less underbidding with extensive feedback. In contrast, the right panel of Figure 7 indicates that the distribution of bids for the largest valuation of 100 ECU with single feedback dominates

that for bids with extensive feedback so that there is less overbidding with extensive feedback for any bidder participating in our experiments. Interestingly, extensive feedback leads a few bidders to submit bids below the equilibrium bid for a value of 100 ECU which we did not observe with single feedback.

To rigorously test for treatment-wise differences between average bids for any given valuation, we employ Mann-Whitney- U -tests, again on the level of independent observations. We find that average bids significantly differ only for the large boundary valuations 90 and 100 ECU (two-tailed, $p \leq 0.0782$). For the smallest boundary valuation 50, the Mann-Whitney- U test slightly misses weak significance ($p = 0.1093$)¹¹, it clearly misses significance ($p \geq 0.2623$) for the valuations 60,70 and 80. If we apply two-tailed t -tests to our data, we find significant differences of average bids for the smallest valuation 50 and the largest valuations 90 and 100 ($p \leq 0.0844$); all other differences of average bids are insignificant ($p \geq 0.2713$). Taken together extensive feedback slightly rotates the average bid function.

TABLE 5: Average bids in the first-price auctions by treatment

valuation	50	60	70	80	90	100	$A(b, \beta^{\text{RNBNE}})$
β^{RNBNE}	50.0	55.0	60.0	65.0	70.0	75.0	0.0
A1G1FP	44.9	54.4	64.0	73.4	83.0	92.0	393.9
	(1.07)	(1.07)	(1.10)	(1.08)	(1.70)	(1.79)	(37.00)
A1G50FP	46.1	55.1	63.8	72.0	80.4	88.5	356.3
	(1.10)	(1.42)	(1.99)	(2.74)	(2.78)	(2.81)	(63.52)

Note: Standard deviations in parenthesis.

We proceed by investigating if the rather weak effect of feedback significantly reduces global deviations from risk-neutral equilibrium. To this end, we measure the distance between observed average bid functions and the risk-neutral equilibrium bid function using the area measure of absolute deviations, see the last column of Table 5. Apparently there are less deviations with extensive feedback. Extensive feedback closes roughly 10% of deviations observed with single feedback. Nevertheless, neither the t -test (two-tailed, $p = 0.2385$) nor the Mann-Whitney- U -test (two-tailed, $p = 0.3367$) identifies a significant feedback effect on deviations from risk-neutral Bayesian Nash equilibrium; further, the finding of insignificant differences between both feedback treatment is supported by a Kolmogorov-Smirnov test ($p = 0.474$). Taken together, the evidence suggests that extensive feedback on multiple auction outcomes is, here, a secondary determinant of bidding behavior. We conclude that our results on the manipulation of risk in first-price

¹¹If we control for learning in the early periods of the experiment and restrict our data set to the second half of the experiment, this difference is significant ($p = 0.025$).

auctions are not distorted by the introduction of extensive feedback into the standard auction setting.

Finding 4. *The introduction of extensive feedback on multiple auction outcomes does not substantially affect bidding behavior in first-price auctions. Extensive feedback slightly rotates the average bid function so that there are less deviations from Bayesian Nash equilibrium with extensive feedback.*

4.2.2 Second-price auctions

For the case of first-price auctions, we observed a weak effect of extensive feedback on average bids at the boundaries of valuation domain. For second-price auctions, there emerges no feedback effect at all at the level of independent observations. This might be due to the fact that feedback is provided for multiple auction outcomes spread over the entire valuation domain where there are typically always some auctions won by any participant while others are lost so that, from the point of Learning Direction Theory (see Selten and Buchta, 1999, Güth et al., 2003), there is no obvious direction for bid adjustment. Table 6 provides average bids conditional on valuations for our second-price treatments with varied feedback condition. Although average bids observed

TABLE 6: Average bids in the second-price auctions by treatment

valuation	50	60	70	80	90	100	$A(b, \beta^{\text{WDS}})$
β^{WDS}	50	60	70	80	90	100	0.0
A1G1SP	53.9 (3.89)	63.6 (4.26)	73.1 (4.39)	82.7 (4.27)	92.3 (4.26)	101.8 (4.55)	324.1 (152.5)
A1G50SP	54.9 (5.80)	64.8 (5.18)	74.5 (4.79)	84.8 (4.83)	94.4 (4.80)	102.6 (6.56)	313.0 (183.1)

Note: Standard deviations in parenthesis.

with extensive feedback (A1G50SP) are roughly 1 ECU larger than those observed with standard feedback (A1G1SP), there is no significant difference in any of the statistical comparisons of average bids separately for each valuation (two-tailed Mann-Whitney- U test: $p > 0.452$; two-tailed t -tests: $p > 0.341$). In both treatments we observe overbidding of the weakly dominant strategy β^{WDS} reflecting the standard finding for second-price auction experiments in our data.

Given no differences between average bids across treatments, it is not surprising that there is no significant difference of global deviations from the weakly dominant strategy and the average bid function between both feedback treatments (two-tailed Mann-Whitney- U test: $p > 0.825$; two-tailed t -tests: $p > 0.893$). Again we employ the area between the average bid function and

the equilibrium bid function, $A(b, \beta^{\text{WDS}})$, to measure global deviations between the average bid function and the weakly dominant strategy (WDS).

4.3 Feedback absorption, complexity, and auction format

The second-price auction may be viewed as less complex for bidders due the existence of a weakly dominant strategy that allows bidders to ignore strategic considerations regarding competitors such as, e.g., the value distribution, inaccurate expectations, or suboptimal response behavior to held expectations. In contrast to standard feedback where a single auction experience is provided, our extensive feedback treatments (A1G50FP and A1G50SP) provide much more feedback. Our experimental setup allows us to investigate whether the opportunity to experience many auction situations with the same bidding strategy is absorbed differently in the less complex second-price auction as compared to absorption in more complex first-price auctions. Since it might be easier for bidders to fruitfully absorb feedback in an easier environment, we specifically hypothesize that the equilibrium deviation is more pronouncedly affected in the less complex second-price auction than in the first-price auction. Figure 8 depicts the evolutions

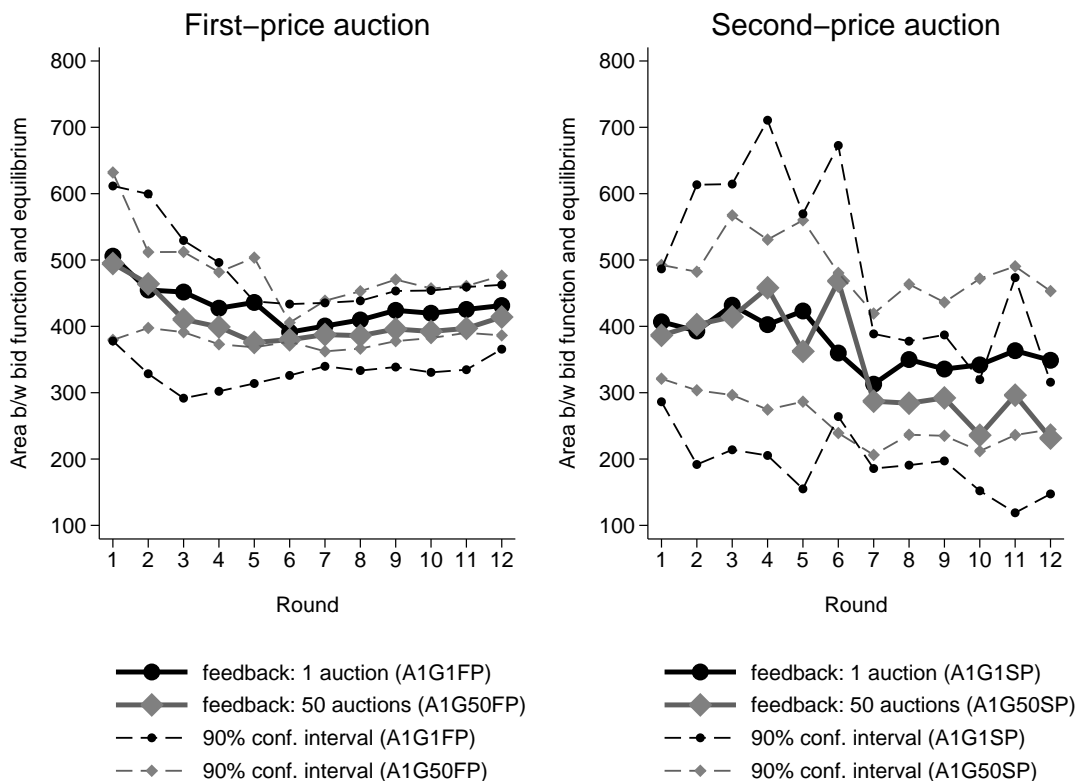


FIGURE 8: Paths of equilibrium deviations over the course of the experiment.

of equilibrium deviations between observed bid functions and the equilibrium bid function on average over the course of the experiment separately for both auction designs. The Figure

also indicates 90% confidence intervals for each path of equilibrium deviations. The left panel illustrates our data for first-price auctions while the right panel pictures second-price auction data. As can be seen from the Figure, our finding that feedback does not substantially change equilibrium deviations in the first-price auction (Finding 4) and in the second-price auction are reproduced for each round since the paths of equilibrium deviation are close to one another for each treatment and also lie within the 90% confidence intervals of either feedback condition.¹²

More importantly, a comparison of equilibrium deviations observed in extensive feedback treatments across auction institutions (grey graph in left panel for A1G50FP vs grey graph in right panel for treatment A1G50SP) suggests that equilibrium deviations are similar only in the beginning of the experiment. While equilibrium deviations in the first-price treatment (A1G50FP) do not change so much over the course of the experiment, equilibrium deviations decrease in the second-price treatment (A1G50SP), particularly towards the end of the experiment. In fact the equilibrium deviation in the first-price auction (A1G50FP) averaged over the final three rounds of the experiment (rounds 10-12) is rather large and amounts to 396.77 EUR. In contrast, the corresponding figure for the second-price auction is only 252.27 EUR. Roundwise comparisons of equilibrium deviations in both treatments (A1G50FP and A1G50SP) reveal statistical differences for the final three rounds ($p \leq 0.0451$) while there are no differences for eight of nine earlier rounds ($p > 0.157$, the exception is round eight with $p = 0.099$.) Since no such difference is observed when comparing the standard-feedback first- and second-price auctions (A1G1FP and A1G1SP), we can assert that:

Finding 5. *There is more feedback absorption leading to less equilibrium deviations in the less complex second-price auction as compared to the more complex first-price auction.*

4.4 How many auction games are necessary to eliminate risk in the standard first-price auction?

To examine how fast risk-induced overbidding is eliminated, we conducted a control experiment (A10G50FP) where round income is determined by only 10 randomly selected auctions out of 50 played auctions. We play 50 auction games altogether to keep feedback constant which facilitates comparisons of the standard risk (A1G50FP) and the reduced risk (A50G50FP) treatments to the control treatment (A10G50FP).

The left panel of Figure 9 compares histograms of individual overbidding in the first-price treatments with reduced risk where 10 auctions are employed, reduced risk where 50 auctions are employed and standard risk (1 auction). The histograms categorize areas between individual

¹²Roundwise comparisons of treatments with standard-feedback (A1G1) to extensive-feedback treatments (A1G50) using the Mann-Whitney U test neither reveal significant differences for first-price auctions ($p \geq 0.149$) nor for second-price auctions ($p \geq 0.123$).

bid functions and the risk-neutral equilibrium bid function, $A_{i,t}^+$. The right panel of Figure 9 provides corresponding empirical distribution functions. With 10 auctions determining round

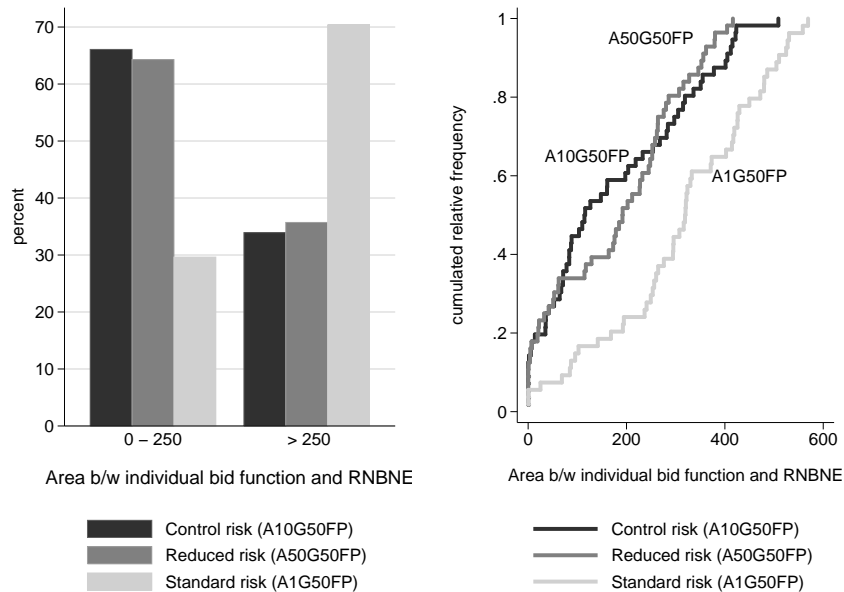


FIGURE 9: Overbidding in first-price auctions: control risk, reduced risk, and standard risk

income, overbidding strongly decreases in a similar way as with 50 auction determining round income. In fact with 10 auctions, large overbidding amounts exceeding 250 ECU fall by 36.4% as compared to the standard-risk treatment. With 50 paid auctions large overbidding decreases by a similar amount, 34.6%. Hence, 10 paid auctions already eliminate the amount of overbidding that is eliminated with 50 paid auctions. Pairwise comparisons of the empirical cumulative distributions functions using a Kolmogorov-Smirnov test reveals no significant differences ($p = 1.000$) between the control risk treatment (10 auctions) and the reduced risk treatment (50 auctions). However, it reveals a significant difference between the control risk treatment and the standard risk treatment ($p = 0.026$).

Figure 10 illustrates average bids for control treatment A10G50FP. Evidently, the introduction of 10 income-relevant auctions shifts the average bid function downward in a similar fashion as the introduction of 50 income-relevant auctions (Fig. 5). In fact, comparing average bids with standard risk (A1G50FP) to those with control risk (A10G50FP) separately for each valuation leads in all cases to significant differences (two-tailed Mann-Whitney- U -tests, $p \leq 0.025$; two-tailed t -tests, $p < 0.01$). In contrast, average bids with control risk (A10G50FP) do not significantly differ from those with reduced risk (A50G50FP) (two-tailed Mann-Whitney- U -tests, $p > 0.109$; two-tailed t -tests, $p > 0.1$) except for the Mann-Whitney- U -test for valuation 50 ($p = 0.0782$).

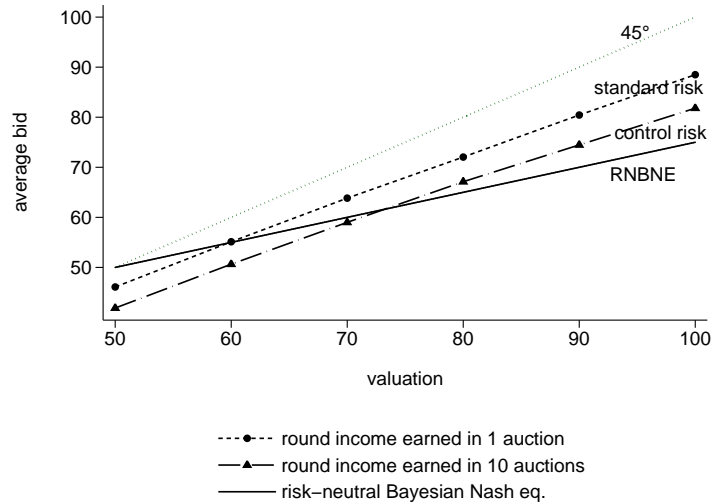


FIGURE 10: Average bid functions in first-price auctions with control risk (10 auctions)

Taken together the removal of risk by paying 10 auctions reduces overbidding observed in standard first-price auctions by a similar amount as the removal of risk by paying 50 auctions. Further, average bids with control risk (A10G50FP) are significantly lower than average bids with standard risk (A1G50FP), while average bids with control risk (A10G50FP) do not significantly differ from those with reduced risk (A50G50FP). Given unknown risk-preferences of subjects in the first place, it is a priori not clear how many auctions are necessary to eliminate risk from the auction setting for a meaningful analysis in the absence of risk. However, we have demonstrated in this section that the choice of 50 paid auctions is rather conservative for eliminating all risk-induced overbidding from the standard auction setting.

5 Conclusion

In this paper we set out to better understand the relation between risk and bidding behavior in auctions. Our goal goes beyond establishing that risk preferences do or do not play a role in bidding. We are interested in assessing the relative importance of risk-preferences compared to other phenomena that may be affecting bidders' behavior. To this end, we introduce a novel experimental design that not only allows us to control and gradually modify the amount of risk that bidders experience in auctions, but also allows us to quantify to which extent deviations from risk-neutral equilibrium bidding are due to risk aversion.

Our procedure for risk-reduction is validated by the fact that reducing risk does not affect bidding behavior in second-price auctions, in which risk-preferences theoretically should not interfere with the weakly dominant equilibrium strategy. We also test for the effect of increased feedback and show that feedback has almost no effect on bidding behavior in first-price auctions

and has only a minor effect on bidding behavior in second-price auctions.

Our main result is that reducing risk reduces the distance between the observed and the risk-neutral equilibrium bid functions. Overall, risk-aversion explains roughly half the amount of overbidding relative to risk-neutral equilibrium in our first-price auction setting. One still has to quantify the descriptive power of the factors that accumulate to the remaining 50% of overbidding relative to the risk-neutral equilibrium prediction. This research agenda, however, goes beyond the purpose of this paper.

Appendix

A Robustness of experimental findings

In this appendix we evaluate the robustness of our findings in two ways. Firstly, we analyze if bidding behavior changes over time, i.e. with experience, and if our findings are robust to behavioral dynamics. Secondly, we investigate if there is heterogeneity in bidding behavior and if individual behavior qualitatively mirrors our aggregate findings.

A.1 Stability of bidding behavior over time

Recent papers on first-price auction experiments report substantial fluctuations of bidding behavior in the beginning periods of first-price auction experiments decreasing over time, see Goeree, Holt, and Palfrey (2002) and Güth et al. (2003). These behavioral dynamics might be due to learning about the rather complex auction setting in early auction periods. Similarly, we find much more intense fluctuations of individual bidding behavior from one period to the next at the beginning of our experiments in all treatments. To quantify the change of submitted bid functions from one round to the next, we measure the distance between average bid functions

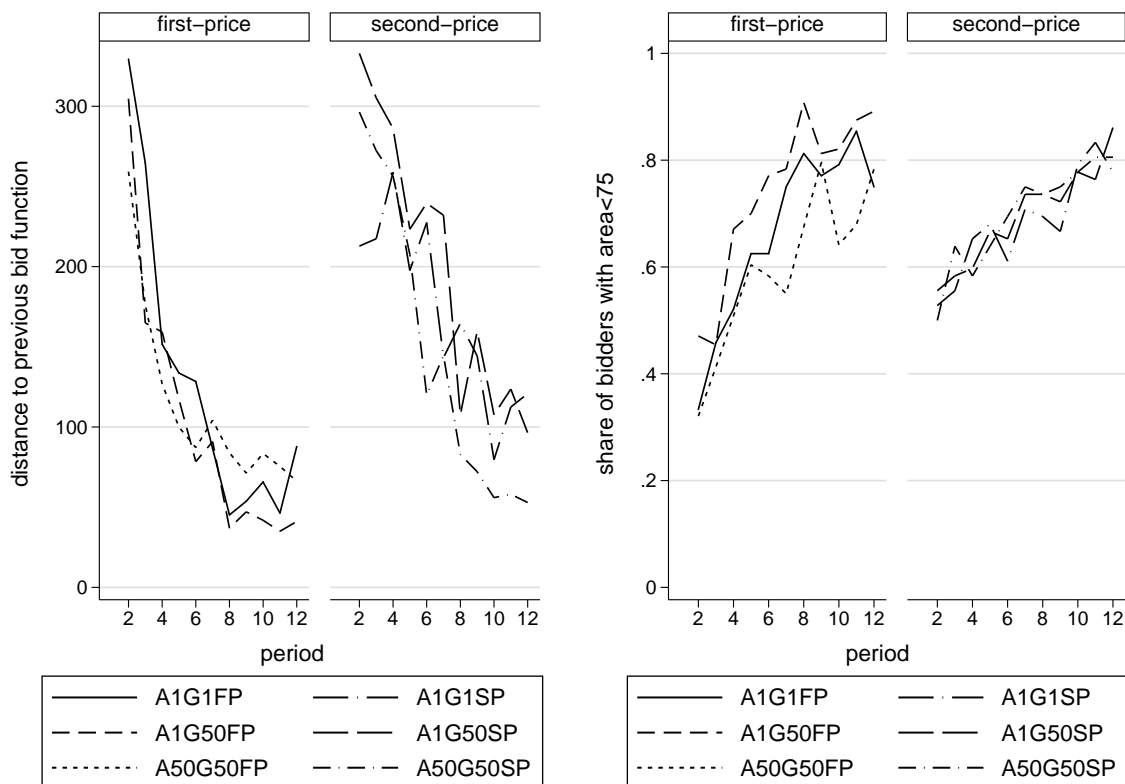


FIGURE 11: Evolution of bidding activity

tions. The distance between average bid functions is given as the area between both functions, $A(b_t, b_{t-1})$. The left part of Figure 11 depicts time paths of the distance between the average bid function submitted in period t and the average bid function that was submitted one period earlier, in period $t - 1$. In the first-price treatments, the average change of bid functions from the first period to the second period is roughly between 250 and 350 ECU. By round eight, the average change rapidly decreased to values between roughly 50 and 75 ECU depending on treatment and period. The evolution of the magnitude of changed bid functions is similar in second-price auctions. Hence, there are a lot of fluctuations in the first few periods that rapidly settle down towards the end of the experiment.

To see if the entire distribution of bidders experiences substantial fluctuations of bidding behavior or if it is rather driven by a minority of bidders, we study the behavior of the share of bidders with small fluctuations of bid functions over time. We consider the change of submitted bid functions from one period to the next as small if the distance measure does not exceed 75 ECU.¹³ The right part of Figure 11 indicates the evolution of the share of bidders with small fluctuations over time in any treatment. Only 30-50% of bidders modestly change their bid functions in the first three periods of the experiment. This number grows over time. Towards the end of the experiment the large majority of bidders, 80-90%, does not create large fluctuations of bid functions.

Overall bidding behavior is much more stable in the second half of the experiment. To investigate if our results reported on the behavioral effects of risk manipulation and extensive feedback are robust to controlling for very intense fluctuations of bidding behavior, we restrict our dataset by excluding data from periods at the beginning of the experiment. In particular we repeat the analysis for data only from the second half of the experiment and another time for data restricted to the last three periods. Restricting datasets in this manner does not qualitatively affect our reported findings. Typically the p -values for the statistical tests with the restricted datasets are smaller when we reported significant differences with the unrestricted data set. We conclude that our findings are robust to changes of bidding behavior over time.

A.2 Individual bidding behavior

Another interesting question is if our aggregate findings on the effects of risk and feedback variations hold on the individual level in general. Firstly, consider the risk effect with first-price auctions. To see if individual bids are generally smaller with reduced risk than with standard risk in the first-price auction, we compute the area below any individual bid function under either risk treatment where individual bids are averaged over all rounds. If the computed area measure is smaller, the underlying individual bid function is closer to the horizontal axis. Thus,

¹³A parallel shift of the bid function by 1.5 ECU leads to a distance of 75 ECU.

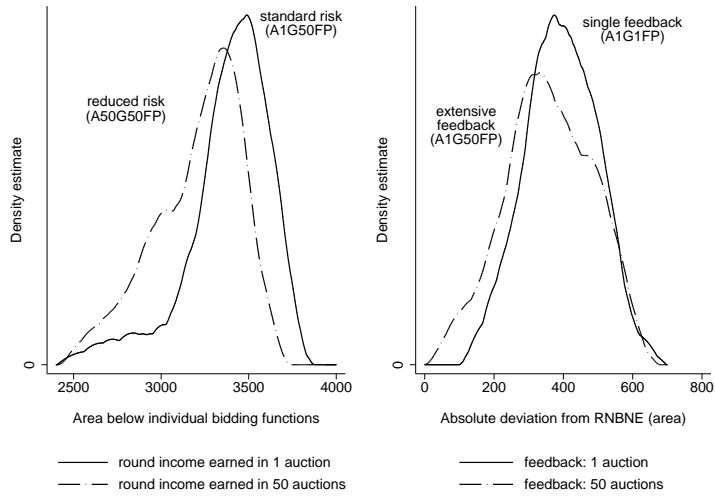


FIGURE 12: Estimated density function of individual effects in first price auctions

a downward movement of individual bid functions can be seen in decreasing values of the area measure. To graphically represent the obtained empirical distributions of area measures, we estimate kernel densities. The left panel of Figure 12 depicts the estimated density functions obtained for the first-price auction. Evidently, the entire distribution appears to shift to the left as risk is reduced so that individuals exhibit smaller area measures with reduced risk. This reflects that the decrease of bids with reduced risk that we reported for the average bidder holds on the individual level, too.

Secondly, consider the feedback effect under first-price auctions where extensive feedback slightly reduces deviations from risk-neutral Bayesian Nash equilibrium. Here, we use the area between individual bid function and the equilibrium bid function to explore effects on individual bidding. As can be seen from the right panel of Figure 12, the density function with extensive feedback exhibits more mass for low deviations from equilibrium in the range of 0 to 300 ECU as compared to the density function with single feedback with more mass for medium deviations in the range of 300 to 600 ECU. It appears that small and medium deviations decrease with extensive feedback.

Under the assumption of independent individual average bid functions, we can use the Kolmogorov-Smirnov test to check for significant differences of distributions. For the first-price auction, the distribution of the area below individual bid functions with standard risk significantly differs from that with reduced risk ($p = 0.000$). In contrast the distribution of equilibrium deviations with single feedback does not significantly differ from that with extensive feedback ($p = 0.146$).

For second-price auctions, we identified neither an effect of manipulations of risk nor feedback on the average level of bid functions. As the left panel of Figure 13 suggests, the entire distri-

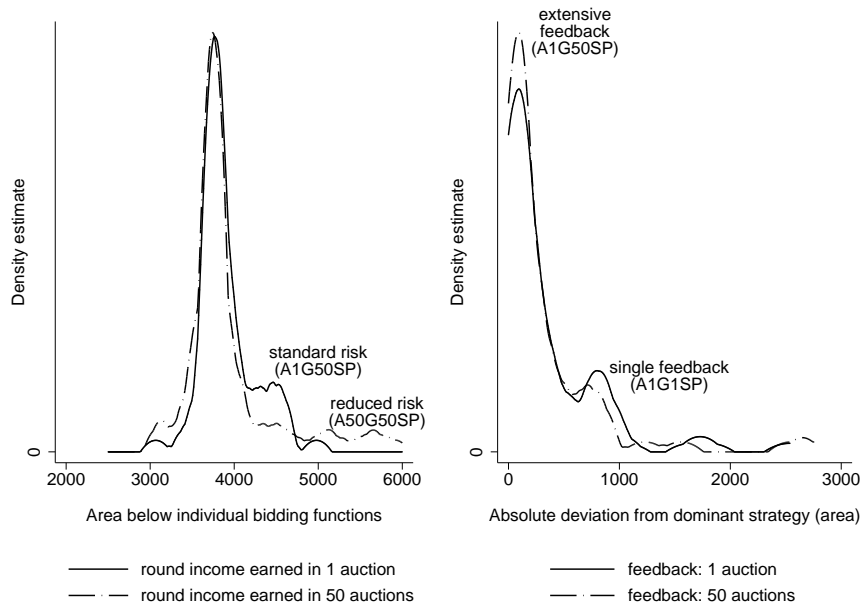


FIGURE 13: Estimated density function of individual effects in first price auctions

bution with standard risk nearly coincides with the distribution with reduced risk; similarly the distributions with single feedback and extensive feedback are almost congruent. Kolmogorov-Smirnov tests under the independence assumption of individual bid functions do not reveal significant differences between distributions (variation of risk: $p = 0.370$; variation of feedback: $p = 0.964$).

B Tabulated data

TABLE 7: Summary statistics of overbidding (area measure) in first-price treatments on independent observation level

treatment	mean	stand. dev.	min	max
A1G50FP	309.3	77.0	164.1	375.9
A50G50FP	178.3	49.8	118.7	255.0

C Experimental Procedures

Participants were recruited by email and could register for the experiment on the internet. At the beginning of the experiment participants drew balls from an urn to determine their allocation to seats. Being seated participants then obtained written instructions. The experiment was computerized and we used the software package z-Tree (Fischbacher, 2007). After answering

control questions on the screen participants entered the treatment described in the instructions. After completing the treatment they answered a short questionnaire on the screen and were paid in cash.

D Instructions

Below we provide instructions for our first-price treatments. Instruction of our second-price treatments were similar. We used identical instructions in treatments A1G50FP, A10G50FP, and A50G50FP. The instructions for A1G1FP were modified slightly to account for the fact that there is feedback on a single auction as opposed to 50 auctions. The instructions are in German. In the following we provide a translation.

D.1 General information

You are participating in a scientific experiment that is sponsored by the state Saxony-Anhalt. If you read the following instructions carefully then you can depending on your decision gain a considerable amount of money. It is, hence, very important that you read the instructions carefully.

The instructions that you have received are only for your private information. **During the experiment no communication is permitted.** Whenever you have questions, please raise your hand. We will then answer your question at your seat. Not following this rule leads to exclusion from the the experiment and all payments.

During the experiment we are not talking about Euro, but about ECU (Experimental Currency Unit). Your entire income will first be determined in ECU. The total amount of ECU that you have obtained during the experiment will be converted into Euro at the end and paid to you in **cash**. The conversion rate will be shown on your screen at the beginning of the experiment.

D.2 Information regarding the experiment

Today you are participating in an experiment on auctions. The experiment is divided into separate rounds. We will conduct **12 rounds**. In the following we explain what happens in each round.

In each round you bid for an object that is being auctioned. Together with you another participant is also bidding for the same object. Hence, in each round, there are **two bidders**. In each round you will be allocated randomly to another participant for the auction. *Your co-bidder in the auction changes in every round.* The bidder with the highest bid obtains the object. If bids are the same the object is allocated randomly.

For the auctioned object you have a valuation in ECU. This valuation lies between 50 and 100 ECU and is determined randomly in each round. The range from 50 to 100 is shown to

you at the beginning of the experiment on the screen and is the same in each round. **From this range you obtain in each round new and random valuations for the object.** The other bidder in the auction also has a valuation for the object. The valuation that the other bidder attributes to the object is determined by the same rules as your valuation and changes in each round, too. All possible valuations of the other bidder are also in the interval from 50 to 100 from which also your valuations are drawn. All valuations between 50 and 100 are equally likely. Your valuations and those of the other player are determined independently. You will be told your valuation in each round. **You will not know the valuation of the other bidder.**

Experimental procedure The experimental procedure is the same in each round and is described in the following. Each round in the experiment has two stages.

1st Stage

In the first stage of the experiment you see the following input screen:

- screenshot of input mode; omitted here -

At that stage **you do not know your own valuation for the object** in this round. On the right side of the screen you are asked to enter a bid for **six hypothetical valuations** that you might have for the object. These six hypothetical valuations are 50, 60, 70, 80, 90, and 100 ECU. Your input into this table will be shown in the graph on the left side of the screen when you click on "draw bids". In the graph the hypothetical valuation is shown on the horizontal axis, the bids are shown on the vertical axis. Your input in the table is shown as six points in the diagram. **Neighbouring points are connected with a line automatically.** These lines determine your bid for all valuations between the six points for which you have made an input. For the other bidder the screen in the first stage looks the same. There are bids for six hypothetical valuations, too. The other bidder can not see your input.

2nd Stage

The actual auction takes place in the second stage of each round. In each round we will play [not in A1G1: not only] a single auction [not in A1G1: but **fifty** auctions]. This is done as follows: [not in A1G1: Fifty times] a random valuation is determined that you have for the object. Similarly for the other bidder [not in A1G1: fifty random valuations are] [in in A1G1: one valuation is] determined. [not in A1G1: The screen lists all auctions ordered by valuations.] You see the following screen:

- screenshot feedback¹⁴; omitted here -

For [only in A1G1: your valuation] [not in A1G1: each of the fifty valuations] the computer determines your bid according to the graph from stage 1. If [in A1G1: your] [not in A1G1: a]

¹⁴The given screenshot for treatment A1G1 differed from that for all other treatments only in the number of displayed auctions. Drawn valuations, bids, and incomes were always replaced by '...' in all instructions.

valuation is precisely at 50, 60, 70, 80, 90, or 100 the computer takes the bid that you gave for this valuation. If [in A1G1: your] [not in A1G1: a] valuation is between these points your bid is determined according to the joining line. In the same way the [in A1G1: bid] [not in A1G1: bids] of the other bidder [in A1G1: is] [not in A1G1: are] determined [not in A1G1: for his fifty valuations]. Your bid is compared with the one of the other bidder. The bidder with the higher bid obtains the object. If you are the bidder with the higher bid, then your income from this auction will be shown. If you are the bidder with the smaller bid, then a dot (.) will be shown instead of the income.

Your income from the auction:

[not in A1FG: A fixed number of auctions out of all 50 auctions will be randomly selected and marked by an asterisk (*). The outcomes of these marked auctions determine your income in this round. All auctions that are not marked do not change your account balance. The number of marked auctions is the same in every round and will be shown on a screen at the start of the experiment.]

[not in A1G1: For each of the randomly selected auctions that are marked by an asterisk (*) the] [only in A1G1: The] following holds:

- The bidder with the higher bid obtains the valuation he had for the object in this auction added to his account minus his bid for the object.
- The bidder with the smaller bid obtains **no income** from this auction.

You total income in a round is [not in A1G1: **the sum of**] **the ECU income from the** [not in A1G1: **marked auctions**] [in A1G1: **auction**] **in this round where you have made the higher bid.**

This ends one round of the experiment and you see in the next round again the input screen from stage 1. At the end of the experiment your total ECU income from all rounds will be converted into Euro and paid to you in cash together with your Show-Up Fee of 3.00 Euro.

Please raise your hand if you have questions.

References

- Abbink, Klaus, Bernd Irlenbusch, Paul Pezanis-Christou, Bettina Rockenbach, and Abdolkarim Sadrieh (2005): An experimental test of design alternatives for the British 3G/UMTS auction, *European Economic Review* 49(2), 505-530.
- Andreoni, James, Yeon-Koo Che, and Jinwoo Kim (2007): Asymmetric information about rival's types in standard auctions: An experiment, *Games and Economic Behavior* 59, 240-259.
- Armantier, Olivier, and Nicolas Treich (2009): Subjective probabilities in games: An application to the overbidding puzzle, *International Economic Review* 50(4), 1079-1102.
- Brosig, Jeannette, and J. Philipp Reiss (2007): Entry decisions and bidding behavior in sequential procurement auctions: An experimental study, *Games and Economic Behavior* 58(1), 50-74.
- Chen, Kay-Yut, and Charles R. Plott (1998), Nonlinear behavior in sealed bid first-price auctions, *Games and Economic Behavior*, 3478.
- Cooper, David J. and Hanming Fang (2008): Understanding Overbidding in Second Price Auctions: An Experimental Study, *Economic Journal*, 118, 1572-1595.
- Cox, James C., Vernon L. Smith, and James M. Walker (1985): Experimental Development of Sealed-Bid Auction Theory: Calibrating Controls for Risk Aversion, *American Economic Review* 75(2), 160-165.
- Cox, James C., Vernon L. Smith, and James M. Walker (1988), Theory and individual behavior of first-price auctions, *Journal of Risk and Uncertainty* 1, 6199.
- Cramton, Peter C. (1995): Money out of thin air: The nationwide narrowband PCS auction, *Journal of Economics and Management Strategy* 4, 267-343.
- Crawford, Vincent P., and Nagore Iriberry (2007): Level-k Auctions: Can a Non-Equilibrium Model of Strategic Thinking Explain the Winner's Curse and Overbidding in Private-Value Auctions?, *Econometrica* 75, 1721-1770.
- Engelbrecht-Wiggans, Richard, and Elena Katok (2008): Regret and Feedback Information in First-Price Sealed-Bid Auctions, *Management Science* 54(4), 808-819.
- Engelbrecht-Wiggans, Richard, and Elena Katok (2007): Regret in Auctions: Theory and Evidence, *Economic Theory* 33, 81-101.

- Engelbrecht-Wiggans, Richard, and Elena Katok (2009): A Direct Test of Risk Aversion and Regret in First Price Sealed Bid Auctions, *Decision Analysis* 6(2), 75-86.
- Filiz-Ozbay, Emel, and Erkut Y. Ozbay (2007): Auctions with Anticipated Regret: Theory and Experiment, *American Economic Review* 97(4), 1407-1418.
- Fischbacher, Urs (2007): z-Tree: Zurich Toolbox for Ready-made Economic Experiments, *Experimental Economics* 10(2), 171-178.
- Garratt, Rod, Walker, Mark, and John Wooders (2008): Behavior in Second-Price Auctions by Highly Experienced eBay Buyers and Sellers, Working Paper.
- Garratt, Rod, and John Wooders (2004): Efficiency in Second-Price Auctions: A New Look at Old Data, Working Paper.
- Goeree, Jacob K., Holt, Charles A., and Thomas Palfrey (2002): Quantal response equilibrium and overbidding in private-value auctions. *Journal of Economic Theory* 104, 247272.
- Güth, Werner, Radosveta Ivanova-Stenzel, Manfred Königstein, and Martin Strobel (2002): Bid functions in auctions and fair division games: experimental evidence. *German Economic Review* 3(4), 461-484.
- Güth, Werner, Radosveta Ivanova-Stenzel, Manfred Königstein, and Martin Strobel (2003): Learning to bid - an experimental study of bid function adjustments in auctions and fair division games, *Economic Journal* 113, 477-494.
- Harstad, Ron (2000): Dominant strategy adoption and bidders' experience with pricing rules, *Experimental Economics* 3, 261-280.
- Isaac, R. Mark, and James M. Walker (1985): Information and Conspiracy in Sealed Bid Auctions, *Journal of Economic Behavior and Organization* 6, 139-159.
- Holt, Charles A. and Susan K. Laury (2002): Risk Aversion and Incentive Effects, *American Economic Review* 92(3), 1644-1655.
- Kagel, John H. (1995): Auctions: a survey, in: Kagel, John H. und Alvin E. Roth (eds.), *Handbook of Experimental Economics*. Princeton: Princeton University Press, 501-585.
- Kagel, John H. and Dan Levin (1993): Independent private values auctions: Bidder behavior in first-, second-, and third-price auctions with varying numbers of bidders, *Economic Journal* 103, 868-879.
- Kagel, John H., Harstad, Ron, and Dan Levin (1987): Information impact and allocation rules in auctions with affiliated private values: a laboratory study, *Econometrica* 55(6), 1275-1304.

- Kirchkamp, Oliver, Poen, Eva, and J. Philipp Reiss (2009): Outside Options: Another reason to choose the first-price auction, *European Economic Review* 53(2), 153-169.
- Kirchkamp, Oliver and J. Philipp Reiss (2010): Heterogeneous bids in auctions with rational and boundedly rational bidders—Theory and Experiment, Working Paper, Maastricht University.
- Maskin, Eric, and John Riley (1984): Optimal auctions with risk averse buyers, *Econometrica* 52, 1473-1518.
- Matthews, Steven A. (1987): Comparing auctions for risk averse buyers: A buyer's point of view, *Econometrica* 55(3), 633-646.
- McMillan, John (1994): Selling Spectrum Rights, *Journal of Economic Perspectives* 8(3), 145-162.
- Milgrom, Paul (2004): *Putting auction theory to work*", Cambridge University Press.
- Morgan, John, Steiglitz, Kenneth, and George Reis (2003): The spite motive and equilibrium behavior in auctions, *Contributions to Economic Analysis & Policy*, 2(1), article 5.
- Neugebauer, Tibor, and Reinhard Selten (2006): Individual behavior in first-price auctions: The importance of information feedback in computerized experimental markets, *Games and Economic Behavior* 54, 183-204.
- Ockenfels, Axel and Reinhard Selten (2005): Impulse Balance Equilibrium and Feedback in First Price Auctions, *Games and Economic Behavior* 51, 155–170.
- Pezanis-Christou, Paul and Abdolkarim Sadrieh (2004): Elicited bid functions in (a)symmetric first-price auctions, Working Paper.
- Rogers, W. H., 1993. Regression standard errors in clustered samples. *Stata Technical Bulletin* 13, 19–23. Reprinted in *Stata Technical Bulletin Reprints* 3, 88–94.
- Roth, Alvin E., and Michael W.K. Malouf (1979), Game-theoretic models and the role of information in bargaining, *Psychological Review* 86, 574-594.
- Selten, Reinhard, and Joachim Buchta (1999): Experimental sealed bid first price auctions with directly observed bid functions. In: (Budescu, D., Erev, I., Zwick, R., eds.) *Games and Human Behavior: Essays in the Honor of Amnon Rapoport*, Mahwah, NJ: Lawrence Erlbaum Associates, 791-802.
- Selten, Reinhard, Abdolkarim Sadrieh, and Klaus Abbink (1999): Money does not induce risk neutral behavior, but binary lotteries do even worse, *Theory and Decision* 46(3), 213-252.

Smith, Vernon L. and James M. Walker (1993): Rewards, Experience and Decision Costs in First Price Auctions, *Economic Inquiry* 31, 237-245.